Advanced concepts in Temporal Point Processes

HUMAN-CENTERED MACHINE LEARNING

http://courses.mpi-sws.org/hcml-ws18/

MAX PLANCK INSTITUTE FOR SOFTWARE SYSTEMS

Temporal Point Processes: Marks and SDEs with jumps

Marked temporal point processes

Marked temporal point process:

A random process whose realization consists of discrete marked events localized in time



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Independent identically distributed marks



Distribution for the marks:

$$x^*(t_i) \sim p(x)$$

Observations:

- 1. Marks independent of the temporal dynamics
- 2. Independent identically distributed (I.I.D.)

Dependent marks: SDEs with jumps



Dependent marks: distribution + SDE with jumps



Distribution for the marks:

$$x^*(t_i) \sim p(x^*|x(t)) \Rightarrow dx(t) = \underbrace{f(x(t), t)dt}_{\text{Drift}} + \underbrace{h(x(t), t)dN(t)}_{\text{Event influence}}$$

- 1. Marks dependent on the temporal dynamics
- 2. Distribution represents additional source of uncertainty

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Mutually exciting + marks



$$dx(t) = \underbrace{f(x(t), t)dt}_{\text{Drift}} + \underbrace{g(x(t), t)dM(t)}_{\text{Neighbor influence}}$$

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Marked TPPs as stochastic dynamical systems

